



Department
for Education

Statistics

GCSE subject content

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The content for statistics GCSE

Introduction

1. The GCSE subject content sets out the knowledge, understanding and skills common to all specifications in GCSE statistics. Together with the assessment objectives it provides the framework within which awarding organisations create the detail of the specification.

Aims and objectives

2. GCSE specifications in statistics must encourage students to develop statistical fluency and understanding through:

- using statistical techniques in a variety of authentic investigations, using real world data in contexts such as, but not limited to, populations, climate, sales etc.
- identifying trends through carrying out appropriate calculations and data visualization techniques
- the application of statistical techniques across the curriculum, in subjects such as the sciences, social sciences, computing, geography, business and economics, and outside of the classroom in the world in general
- critically evaluating data, calculations and evaluations that would be commonly encountered in their studies and in everyday life
- understanding how technology has enabled the collection, visualisation and analysis of large quantities of data to inform decision- making processes in public, commercial and academic sectors
- applying appropriate mathematical and statistical formulae, as set out in Appendix 1, and building upon prior knowledge, as listed in Appendix 2

Subject content

Overview

3. The subject content sets out the full range of content for GCSE specifications in statistics. Awarding organisations may, however, use any flexibility to increase depth, breadth or context within the specified topics or to consolidate teaching of the subject content.
4. Specifications should ensure students develop the confidence and competence with statistical techniques that enable them to apply those techniques flexibly to solve statistical problems through a practical programme of study.
5. The expectation of the GCSE statistics content is that:
 - all students will develop confidence and competence with the content identified by standard type
 - all students will be assessed on the content identified by the standard and the underlined type in curly brackets, underlined type in curly brackets will be included in both foundation and higher papers; more highly attaining students will develop confidence and competence with all of this content
 - only the more highly attaining students will be assessed on the content identified by bold type and in square brackets; the highest attaining students will develop confidence and competence with this content
6. The distinction between standard, underlined type in curly brackets and bold type in square brackets applies to the content statements only, not to the assessment objectives or to the statistical enquiry cycle and prior knowledge in the appendices.
7. Statistics is a practical subject and specifications must make explicit reference to how the assessment will focus on the underpinning principles of the statistical enquiry cycle, as detailed in Appendix 3, developed through practical investigations completed as part of the programme of study. Specifications should give students the opportunity to understand that different approaches, including the use of technology, may be appropriate at each stage of the statistical enquiry cycle, and that statistical conclusions are developed through an iterative process of retesting and refinement. Specifications should give students the opportunity to develop an understanding of how the subject content is applied in decision making processes used in the world around them by using realistic data taken from authentic contexts in their studies.

Detailed subject content

8. GCSE specifications in statistics must require students to:

A	Understand the importance of the careful planning of a clear strategy for collecting, recording and processing data in order to address an identified question or hypothesis
A1	Know that a hypothesis can only be tested through the appropriate collection and analysis of data. Formal use of null hypothesis will not be required
A2	Know the constraints that may be faced in designing an investigation to test an hypothesis: these may include factors such as time, costs, ethical issues, confidentiality, and convenience, etc.
A3	Determine proactive strategies to mitigate issues that might arise during the statistical enquiry process. For example, dealing with difficulties in identifying the population, non-response issues or unexpected outcomes

B	Recognise the opportunities, constraints and implications for subsequent mathematical analysis involved in obtaining appropriate data through careful design of primary data collection techniques or through the use of reference sources for secondary data to ensure unbiased research
B1	Know and apply terms used to describe different types of data that can be collected for statistical analysis: raw data, { <u>quantitative, qualitative</u> }, categorical, ordinal, discrete, continuous, ungrouped, grouped, { <u>bivariate</u> } and [multivariate] Know the advantages and implications of merging data into more general categories, and of grouping numerical data into class intervals { <u>Know and apply the terms explanatory or independent variables and response or dependent variables</u> }
B2	Know the difference between primary and secondary data Know that data can be collected from different sources: experimental (laboratory, field and natural), simulation, questionnaires, observation, reference, census, population and sampling and that sources of secondary data should be acknowledged { <u>Know the importance of reliability and validity with regards to collected data</u> } { <u>Determine factors that may lead to bias, including issues of sensitivity of the content matter, and know how to minimise data distortion</u> }, [including level of control]
B3	Know the difference between population, sample frame and sample Know that “population” can have different meanings within a stated context Know reasons for employing judgement or opportunity (convenience) sampling, and the associated risks of bias when these techniques are used Use appropriate sampling techniques in the context of the problem to avoid bias: random, systematic, and { <u>quota</u> } Know the key features of a simple random sample { <u>and demonstrate understanding of how different techniques, both physical and electronic, are used to select random members from a population: including, but not limited to, dice, cards, random number lists, and calculator functions</u> } { <u>Use stratification and know when this is appropriate before sampling takes place</u> }

B4	Know the key features to be considered when planning data collection: leading questions, avoiding biased sources, time factors, open/closed questions, different types of interview technique
B5	Know and demonstrate understanding of techniques used to deal with problems that may arise with collected data: for example, missing data, incorrect formats, non-responses, incomplete responses, etc. Know why data may need to be “cleaned” before further processing, including issues that arise on spreadsheets and apply techniques to clean data in context <u>{Know the importance of identifying and controlling extraneous variables}</u> [and the use of control groups]

C	Generate data visualisation and understand the mathematics required to derive these visualisations
C1	Represent data sets pictorially using calculated key values as necessary, and interpret and compare data sets displayed pictorially: tabulation, tally, pictogram, <u>{pie chart, stem and leaf diagram, Venn diagram}</u> Interpret and compare data sets displayed pictorially: <u>{population pyramid, choropleth map}</u> , [comparative pie chart, comparative 2D representations, comparative 3D representations]
C2	Represent data sets graphically using calculated key values as necessary, and interpret and compare data sets displayed graphically: bar charts, line charts, time series, scatter charts, <u>{bar line charts, frequency polygons, cumulative frequency (discrete and grouped) charts, histograms (equal width), and box plots}</u> [Calculate and use frequency density to draw histograms (unequal width), and interpret and compare data sets displayed in histograms (unequal width)]
C3	Justify the appropriate format and produce accurate visualisation of data Recognise where errors in construction lead to graphical misrepresentation, including but not limited to incorrect scales, truncated axis, distorted sizing [or the misuse of formula when calculating the frequency densities of histograms]
C4	Extract and calculate corresponding values in order to compare data sets that have been presented in different formats and be able to present the same information in multiple formats Select <u>{and justify}</u> appropriate form of representation <u>{with regard to the nature of data}</u>

D	Calculate statistical measures to compare data
D1	Calculate averages for discrete and grouped data: mode, median, arithmetic mean, [weighted mean, geometric mean, mean seasonal variation] <u>{Justify the rationale for selecting appropriate types of average in context}</u>
D2	Determine skewness from data by inspection [and by calculation. Formula to be given when required]
D3	Calculate different measures of spread: range, quartiles, <u>{interquartile range, percentiles}</u> , [interpercentile range, interdecile range and standard deviation] Identify outliers by inspection [and using appropriate calculations]

D4	Identify trends in data through inspection {and by calculation of 4 [or other determined appropriate] <u>point moving averages</u> }
D5	Determine line of best fit by eye, { <u>by drawing through a calculated double mean point (\bar{x}, \bar{y})</u> } [and by using the equation of the regression line]
D6	[Apply formula to determine Spearman's rank correlation coefficient. Values found using calculator functions will be permissible]
D7	Use collected data to calculate estimates of probabilities

E	Use visualisation and calculation to interpret results with reference to the context of the problem, and to evaluate the validity and reliability of statistical findings
E1	Compare the probability of different possible outcomes using the 0-1 or 0- 100% scale Use probability values to calculate expected frequency of a specified characteristic within a sample or population <u>{Use collected data and calculated probabilities to determine and interpret relative risks and absolute risks, and express in terms of expected frequencies in groups}</u>
E2	Compare experimental data with theoretical predictions to identify possible bias within the experimental design Recognise that experimental probability will tend towards theoretical probability as the number of trials increases when all variables are random <u>{Use two-way tables, sample space diagrams, tree diagrams and Venn diagrams to represent all the different outcomes possible for at most three events}</u>
E3	Compare different data sets using appropriate calculated or given measure of central tendency: mode, modal group, median and mean Compare different data sets using appropriate calculated or given measure of spread: range, {interquartile range, percentiles } [and standard deviation] <u>{Use calculated or given median and interquartile range} [or interpercentile range or interdecile range or mean and standard deviation] {to compare data samples and to compare sample data with population data}</u>
E4	<u>{Know and apply the formal notation for independent events}</u> <u>{Know and apply the formal notation for conditional probability}</u>
E5	Interpret a distribution of data in terms of skewness identified from inspection [or calculation] <u>{Comment on outliers with reference to the original data}</u>
E6	<u>{Interpret seasonal and cyclic trends in context}</u> [Use such trends to make predictions]
E7	Interpret data related to rates of change over time (including, but not limited to, births, deaths, house prices, and unemployment) when given in graphical form. <u>{Calculate and interpret rates of change over time from tables using context specific formula}</u> <u>{Use different types of index [and weighted index] numbers in context, including but not limited to retail price index, consumer price index and gross domestic product}</u>

E8	<p>Know and apply vocabulary of correlation: positive, negative, zero, causation, association, interpolation and extrapolation</p> <p>Make comparisons of correlation by inspection: strong or weak</p> <p><u>{Know that correlation does not necessarily imply causation}</u></p> <p>[Know that there are multiple factors that may interact]</p>
E9	<p><u>{Interpret} [calculated or] {given Spearman's rank correlation coefficient in the context of the problem}</u></p> <p>[Interpret given Pearson's product moment correlation coefficient in the context of the problem]</p> <p>[Understand the distinction between Spearman's rank correlation and Pearson's product moment correlation coefficients]</p>
E10	<p>[Comment on the differences between experimental and theoretical values in terms of possible bias. Formal tests of significance will not be required]</p> <p>[Know and interpret the characteristics of a binomial distribution]</p>
E11	<p>[Know and interpret the characteristics of a Normal distribution]</p> <p>[Know that, for a Normal distribution, values more than three standard deviations from the mean are very unusual; know that approximately 95% of the data lie within two standard deviations of the mean and that 68% (just over two thirds) lie within one standard deviation of the mean]</p> <p>[Use action and warning lines in quality assurance sampling applications]</p> <p>[Use calculated or given means and standard deviation to standardise and interpret data collected in two comparable samples. Formulae will be given]</p>
E12	<p><u>{Use calculated or given summary statistical data to make estimates of population characteristics. Use samples to estimate population mean. Use sample data to predict population proportions}</u></p> <p>[Apply Petersen capture/recapture formula to calculate an estimate of the size of a population]</p>
E13	<p>Know that sample size has an impact on reliability and replication</p> <p>[Know that a set of sample means are more closely distributed than individual values from the same population]</p>

Appendix 1 - formulae

Foundation tier

Formulae included in the GCSE Mathematics subject content. Students are expected to know these formulae; they must not be given in the assessment.

Specification reference	Formula required
B3	In order to carry out stratification, calculating the percentage or proportion of an amount: $\frac{x}{100} \times \text{amount}$
C1	Calculating the angle for a sector in a pie chart: $\frac{x}{\text{total}} \times 360$
C2	Frequency density for a histogram: $\text{frequency density} = \frac{\text{frequency}}{\text{classwidth}}$
D1	Calculation of arithmetic mean: $\bar{x} = \frac{\sum fx}{\sum f}$
D3	Range = highest value – lowest value
D3	Interquartile range (IQR) = upper quartile – lower quartile
D7	Probability = $\frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}}$

Formulae included in the subject content. Students are expected to know these formulae; they must not be given in the assessment.

Specification reference	Formula required
D4	4 point moving average = $\frac{x_1 + x_2 + x_3 + x_4}{4}$
D5	Calculate double mean point (\bar{x}, \bar{y}) : $\bar{x} = \frac{\sum fx}{\sum f}, \bar{y} = \frac{\sum fy}{\sum f}$

E4	Formulae for independent events: $P(A \text{ and } B) = P(A) \times P(B)$ $P(A B) = P(A)$ $P(B A) = P(B)$
E4	Formula for conditional probability $P(B A) = \frac{P(A \text{ and } B)}{P(A)}$
E7	$\text{IndexNumber} = \frac{\text{current value of item}}{\text{value in base year}} \times 100$

Formulae that students should be able to use, but need not memorise. These can be given in the assessment, either in the appropriate question, or in a list from which students select and apply as appropriate.

Specification reference	Formula required
E7	Rates of change (e.g. Birth rate = $\frac{\text{number of births} \times 1000}{\text{total population}}$)

Higher tier

Formulae included in the GCSE Mathematics subject content. Students are expected to know these formulae; they must not be given in the assessment.

Specification reference	Formula required
B3	In order to carry out stratification, calculating the percentage or proportion of an amount: $\frac{x}{100} \times \text{amount}$
C1	Calculating the angle for a sector in a pie chart: $\frac{x}{\text{total}} \times 360$
C2	Frequency density for a histogram: $\text{frequency density} = \frac{\text{frequency}}{\text{classwidth}}$
D1	Calculation of arithmetic mean: $\bar{x} = \frac{\sum fx}{\sum f}$
D3	Range = highest value – lowest value

D3	Interquartile range (IQR) = upper quartile – lower quartile
D7	Probability = $\frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}}$

Formulae included in the subject content. Students are expected to know these formulae; they must not be given in the assessment.

Specification reference	Formula required
C1	Calculating the radius of a circle for a proportional pie chart: $r = \sqrt{\frac{\text{newtotal} \times \text{oldradius}^2}{\text{oldtotal}}}$
D1	Calculation of weighted mean: $\text{weighted mean} = \frac{\sum(\text{value} \times \text{weight})}{\sum \text{weights}}$
D1	Geometric mean = $\sqrt[n]{\text{value}_1 \times \text{value}_2 \times \dots \times \text{value}_n}$
D3	Interpercentile range and interdecile range as appropriate: percentile 1 – percentile 2 (calculation of a percentage needed as in B3 above)
D3	Identification of an outlier: Small outlier is < LQ – 1.5IQR Large outlier is > UQ + 1.5IQR Outlier is also outside $\mu \pm 3\sigma$
D4	Moving averages (m.a.) n point moving average: $\text{m.a.} = \frac{x_1 + x_2 + \dots + x_n}{n}$
D5	Calculate double mean point (\bar{x}, \bar{y}) : $\bar{x} = \frac{\sum fx}{\sum f}, \bar{y} = \frac{\sum fy}{\sum f}$
E4	Formulae for independent events: $P(A \text{ and } B) = P(A) \times P(B)$ $P(A B) = P(A)$ $P(B A) = P(B)$
E4	Formula for conditional probability $P(B A) = \frac{P(A \text{ and } B)}{P(A)}$

E7	Index number = $\frac{\text{current value of item}}{\text{value in base year}} \times 100$
E7	Weighted index number = $\frac{\sum(\text{index} \times \text{weight})}{\sum \text{weights}}$
E13	Peterson capture recapture formula: Number in population = $\frac{\text{sample size 1} \times \text{sample size 2}}{\text{number marked in sample 2}}$

Formulae that students should be able to use, but need not memorise. These can be given in the assessment, either in the appropriate question, or in a list from which students select and apply as appropriate.

Specification reference	Formula required
D2	Skew = $\frac{3(\text{mean} - \text{median})}{\text{standard deviation}}$
D3	Standard deviation = $\sqrt{\frac{1}{N} \sum (x - \mu)^2}$ alternate formula Standard deviation = $\sqrt{\frac{\sum x^2}{N} - \left(\frac{\sum x}{N}\right)^2}$
D6	Spearman's rank correlation coefficient $r_s = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$
E7	Rates of change (e.g. Birth rate = $\frac{\text{number of births} \times 1000}{\text{total population}}$)

Appendix 2 – prior knowledge

Integers, fractions, decimals and percentages

- work interchangeably with terminating decimals and their corresponding fractions (such as 3.5 and $\frac{7}{2}$ or 0.375 and $\frac{3}{8}$). Recognise that some fractions can be written as recurring decimals
- identify and work with fractions in ratio problems
- interpret fractions and percentages as operators

Structure and calculation

- order positive integers, decimals and fractions
- understand and use the symbols =, \neq , <, >, \leq , \geq
- apply the four operations to integers, decimals and simple fractions (proper and improper), and mixed numbers
- understand and use place value (e.g. when working with very large or very small numbers, and when calculating with decimals)
- understand and use standard form
- recognise and use relationships between operations, including inverse operations e.g. cancellation to simplify calculations and expressions; use conventional notation for priority of operations, including brackets, powers, roots and reciprocals
- substitute numerical values into formulae and expressions, including scientific formulae
- understand and use standard mathematical formulae; rearrange formulae to change the subject
- work with coordinates on Cartesian grid

Measures and accuracy

- use standard units of mass, length, time, money and other measures (including standard compound measures) using decimal quantities where appropriate
- estimate answers; check calculations using approximation and estimation, including answers obtained using technology
- use compound units such as speed, rates of pay, unit pricing
- round numbers and measures to an appropriate degree of accuracy (e.g. to a specified number of decimal places or significant figures); use inequality notation to specify simple error intervals due to truncation or rounding

Ratio, proportion and rates of change

- express one quantity as a fraction of another, where the fraction is less than 1 or greater than 1
- use ratio notation, including reduction to simplest form
- divide a given quantity into two parts in a given part:part or part:whole ratio; express the division of a quantity into two parts as a ratio; apply ratio to real contexts and problems (such as those involving probability)
- relate ratios to fractions and vice versa
- define percentage as 'number of parts per hundred'; interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively; express one quantity as a percentage of another; compare two quantities using percentages
- understand and use the general equation of a straight line $y = mx + c$ where c is the

intercept with the y - axis and $m = \frac{(y_1 - y_2)}{(x_1 - x_2)}$

Appendix 3 - statistical enquiry cycle

Specifications must encourage the application of techniques within the framework of the statistical enquiry cycle using real data taken from authentic contexts.

Specifications must require students to understand the importance of initial planning when designing a line of enquiry or investigation including:

- defining a question or hypothesis (or hypotheses) to investigate
- deciding what data to collect and how to collect and record it giving reasons
- developing a strategy for how to process and represent the data giving reasons

Specifications must enable students to recognise the constraints involved in sourcing appropriate data including:

- when designing collection methods for primary data
- when researching sources of secondary data, including from reference publications, the internet and the media
- through appreciating the importance of acknowledging sources
- by recognising where issues of sensitivity may influence data availability

Specifications must require students to understand the ways that data can be processed and presented including:

- organising and processing data, including an understanding of how technology can be used
- generating diagrams and visualisations to represent the data, including an understanding of outputs generated by appropriate technology
- generating statistical measures to compare data, understanding the advantages of using technology to automate processing

Specifications must require students to understand that results must be interpreted with reference to the context of the problem including:

- analysing/interpreting the diagrams and calculations/measures
- reaching conclusions that relate to the questions and hypotheses addressed
- making inferences and/or predictions
- discussing the reliability of findings

Specifications must require students to show an understanding of the importance of the clear and concise communication of findings and key ideas, and awareness of target audience.

Specifications must enable students to understand the importance of evaluating statistical work including:

- identifying weaknesses in approach or representation
- suggesting improvements to processes or the presentation
- refining the process to elicit further clarification of the initial hypothesis



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