National curriculum tests

Key stage 2

Mathematics test framework

National curriculum tests from 2016

For test developers



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1. Overview

This test framework is based on the national curriculum programme of study (2014) for mathematics, introduced for teaching in schools from September 2014 and first assessed in summer 2016. The framework specifies the purpose, format, content and cognitive domains of the key stage 2 mathematics tests; it is not designed to be used to guide teaching and learning or to inform statutory teacher assessment.

This document has been produced to aid the test development process.

1.1 Purposes of statutory assessment

The main purpose of statutory assessment is to ascertain what pupils have achieved in relation to the attainment targets outlined in the national curriculum (2014) in mathematics.

The main intended uses of the outcomes as set out in the Bew Report and the Government's consultation document on primary assessment and accountability are to:

- hold schools accountable for the attainment and progress made by their pupils
- inform parents and secondary schools about the performance of individual pupils
- enable benchmarking between schools, as well as monitoring performance locally and nationally

2. What is a test framework?

The purpose of the test framework is to provide the documentation to guide the development of the tests. The framework is written primarily for those who write test materials and to guide subsequent development and test construction. It is being made available to a wider audience for reasons of openness and transparency.

Some elements of the statutory national curriculum are not possible to assess using the current form of testing; they will need to be assessed by teachers as part of their statutory assessment of the complete national curriculum.

The framework includes those parts of the programme of study as outlined in the national curriculum (2014) that will be covered in the test (the content domain). The cognitive processes associated with the measurement of mathematics are also detailed in the cognitive domain.

The test framework also includes a test specification from which valid, reliable and comparable tests can be constructed each year. This includes specifics about test format, question types, response types, marking and a clear test-level reporting strategy.

By providing all of this information in a single document, the test framework answers questions about what the test will cover, and how, in a clear and concise manner. The framework does not provide information on how teachers should teach the national curriculum.

The test development process used by the Standards and Testing Agency (STA) embeds within it the generation of validity and reliability evidence through expert review and trialling. Given the nature of the evidence collected, it is not anticipated that any additional studies will be required in order to demonstrate that the tests are fit for purpose. The test framework does not provide detail of the validity and reliability of individual tests; this will be provided in the test handbook, which will be published on the DfE's website following the administration of the test.

The test framework should be used in conjunction with the national curriculum (2014) and the annual 'Assessment and reporting arrangements' (ARA) document.

3. Nature of the test

The key stage 2 mathematics test forms part of the statutory assessment arrangements for pupils at the end of key stage 2.

The test is based on the relevant sections of the national curriculum statutory programme of study (2014) for mathematics at key stage 2.

The test will cover the aspects of the curriculum that lend themselves to paper-based, externally marked testing.

3.1 Population to be assessed

All eligible pupils who are registered at maintained schools, special schools, or academies (including free schools) in England and are at the end of key stage 2 will be required to take the key stage 2 mathematics test, unless they have taken it in the past.

Some pupils are exempt from the tests. Further details are in the ARA, which can be found on the GOV.UK website at www.gov.uk/sta.

3.2 Test format

The key stage 2 mathematics test comprises two components, which will be presented to pupils as three separate test papers. The first component is an arithmetic paper. The second component is administered as two papers; there are no significant differences in format between the two papers. The test is administered on paper and the total testing time is 110 minutes.

Table 1: Format of the test

Component	Description	Number of papers	Number of marks	Timing of component
Paper 1: arithmetic	arithmetic assesses pupils' confidence with the range of mathematical operations	1	40	30 minutes
Paper 2 and Paper 3: mathematical reasoning	mathematical fluency, solving mathematical problems and mathematical reasoning	2	70 overall 35 per paper	80 minutes 40 minutes per paper
	Total	3	110	110 minutes

3.3 Resource list

The resource list for the mathematics tests comprises pencil / black pen, eraser, ruler (mm and cm), angle measurer / protractor and mirror. Pupils will not be permitted to use a calculator in any of the components.

4. Content domain

The content domain sets out the relevant elements from the national curriculum programme of study (2014) for mathematics at key stage 2 that are assessed in the mathematics test. The tests will, over time, sample from each area of the content domain.

The content domain also identifies elements of the programme of study that cannot be assessed in the key stage 2 tests (section 4.3). Attainment in these elements will be monitored through teacher assessment.

Tables 2 and 3 detail content from the national curriculum (2014). Elements from the curriculum are ordered to show progression across the years. The curriculum has been grouped into subdomains and these are detailed in the strand column.

4.1 Content domain referencing system

A referencing system is used in the content domain to indicate the year, the strand and the sub-strand, for example '3N1' equates to:

- year 3
- strand Number and place value
- sub strand 1

Table 2 shows the references for the strands and sub-strands and Table 3 shows the progression across the years.

Table 2: Content domain strands and sub-strands

Strand	Sub-strand	Content domain reference
Number and place value	counting (in multiples)	N1
value	read, write, order and compare numbers	N2
	place value; roman numerals	N3
	identify, represent and estimate; rounding	N4
	negative numbers	N5
	number problems	N6

Strand	Sub-strand	Content domain reference
Addition, subtraction,	add / subtract mentally	C1
multiplication and division (calculations)	add / subtract using written methods	C2
	estimate, use inverses and check	C3
	add / subtract to solve problems	C4
	properties of number (multiples, factors, primes, squares and cubes)	C5
	multiply / divide mentally	C6
	multiply / divide using written methods	С7
	solve problems (commutative, associative, distributive and all four operations)	C8
	order of operations	С9
Fractions, decimals	recognise, find, write, name and count fractions	F1
and percentages	equivalent fractions	F2
	comparing and ordering fractions	F3
	add / subtract fractions	F4
	multiply / divide fractions	F5
	fractions / decimals equivalence	F6
	rounding decimals	F7
	compare and order decimals	F8
	multiply / divide decimals	F9
	solve problems with fractions and decimals	F10
	fractions / decimal / percentage equivalence	F11
	solve problems with percentages	F12
Ratio and proportion	relative sizes, similarity	R1
	use of percentages for comparison	R2
	scale factors	R3
	unequal sharing and grouping	R4

Strand	Sub-strand	Content domain reference
Algebra	missing number problems expressed in algebra	A1
	simple formulae expressed in words	A2
	generate and describe linear number sequences	А3
	number sentences involving two unknowns	A4
	enumerate all possibilities of combinations of two variables	А5
Measurement	compare, describe and order measures	M1
	estimate, measure and read scales	M2
	money	М3
	telling time, ordering time, duration and units of time	M4
	convert between metric units	M5
	convert metric / imperial	M6
	perimeter, area	M7
	volume	M8
	solve problems (a, money; b, length; c, mass / weight; d, capacity / volume)	M9
Geometry – properties	recognise and name common shapes	G1
of shapes	describe properties and classify shapes	G2
	draw and make shapes and relate 2–D to 3–D shapes (including nets)	G3
	angles – measuring and properties	G4
	co-ordinates	G5
Geometry – position	patterns	P1
and direction	describe position, direction and movement	P2
	co-ordinates	Р3
Statistics	interpret and represent data	S 1
	solve problems involving data	S2
	mean average	S3

4.2 Content domain for key stage 2 mathematics

Table 3: Content domain

7				Content domain reference	ain refe	rence		
Strand		Year 3		Year 4		Year 5		Year 6
Number and place value	3N1b	count from 0 in multiples of 4, 8, 50 and 100	4N1	count in multiples of 6, 7, 9, 25 and 1000	5N1	count forwards or backwards in steps of powers of 10 for any given number up to 1000 000		
	3N2a	compare and order numbers up to 1000 read and write numbers to 1000 in numerals and in words	4N2a	order and compare numbers beyond 1000	5N2	read, write, order and compare numbers to at least 1 000 000	6N2	read, write, order and compare numbers up to 10000000
	3N2b	find 10 or 100 more or less than a given number	4N2b	find 1000 more or less than a given number				
	3N3	recognise the place value of each digit in a three-digit number (hundreds, tens, ones)	4N3a	recognise the place value of each digit in a four- digit number (thousands, hundreds, tens and ones)	5N3a	determine the value of each digit in numbers up to 1 000 000	6N3	determine the value of each digit in numbers up to 10000000
			4N3b	read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value	5N3b	read Roman numerals to 1000 (M) and recognise years written in Roman numerals		
	3N4	identify, represent and estimate numbers using different representations	4N4a	identify, represent and estimate numbers using different representations				

-				Content domain reference	ain ref	erence		
Strand		Year 3		Year 4		Year 5		Year 6
Addition, subtraction, multiplication and division (calculations) (continued)	3C3	estimate the answer to a calculation and use inverse operations to check answers	4C3	estimate and use inverse operations to check answers to a calculation	5C3	use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy	6G3	use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
	3C4	solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	4C4	solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	5C4	solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why	6C4	solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
					5C5a	identify multiples and factors, including finding all factor pairs of a number and common factors of two numbers	6C5	identify common factors, common multiples and prime numbers
					5C5b	know and use the vocabulary of prime numbers, prime factors and composite (nonprime)		
					5C5c	establish whether a number up to 100 is prime and recall prime numbers up to 19		
					5C5d	recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³)		

				Content domain reference	nain refe	rence		
Strand		Year 3		Year 4		Year 5		Year 6
Addition, subtraction, multiplication and division (calculations)	3C6	recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables	4C6a	recall multiplication and division facts for multiplication tables up to 12 × 12	5C6a	multiply and divide numbers mentally drawing upon known facts	929	perform mental calculations, including with mixed operations and large numbers
(nean in 100)			4C6b	use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers	5C6b	multiply and divide whole numbers and those involving decimals by 10, 100 and 1000		
			4C6c	recognise and use factor pairs and commutativity in mental calculations				
	3C7	write and calculate mathematical statements for multiplication and division using the multiplication tables that pupils know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods	4C7	multiply two-digit and three-digit numbers by a one-digit number using formal written layout	5C7a	multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two- digit numbers	6C7a	multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication

		Content domain reference	in reference	
Strand	Year 3	Year 4	Year 5	Year 6
Addition, subtraction, multiplication and division (calculations) (continued)			divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context	divide numbers up to 4 digits by a two- digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
				divide numbers up to 4 digits by a two- digit number using the formal written method of short division where appropriate, interpreting remainders according to
	including missing number problems, including missing number problems, involving multiplication and division, including integer scaling problems and correspondence problems in which nobjects are connected to mobjects	involving multiplying and adding, including and adding, including using the distributive law to multiply twodigit numbers by one digit numbers by one digit, integer scaling problems and harder correspondence problems such as nobjects are connected to mobjects	solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes	6C8 solve problems involving addition, subtraction, multiplication and division

				Content domain reference	ain ref	irence		
Strand		Year 3		Year 4		Year 5		Year 6
Fractions, decimals and percentages (continued)	3F1c	recognise and use fractions as numbers: unit fractions and non- unit fractions with small denominators						
	3F2	recognise and show, using diagrams, equivalent fractions with small denominators	4F2	recognise and show, using diagrams, families of common equivalent fractions	5F2a	recognise mixed numbers and improper fractions and convert from one form to the other; write mathematical statements > 1 as a mixed number [e.g. $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1 + \frac{1}{5}$]	6F2	use common factors to simplify fractions; use common multiples to express fractions in the same denomination
					5F2b	identify name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths		
	3F3	compare and order unit fractions and fractions with the same denominators			5F3	compare and order fractions whose denominators are all multiples of the same number	6F3	compare and order fractions, including fractions >1
	3F4	add and subtract fractions with the same denominator within one whole [e.g. $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$]	4F4	add and subtract fractions with the same denominator	5F4	add and subtract fractions with the same denominator and denominators that are multiples of the same number	6F4	add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions

		Content domain reference	ain refe	rence		
Strand	Year 3	Year 4		Year 5		Year 6
Fractions, decimals and percentages (continued)			5F5	multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	6F5a	multiply simple pairs of proper fractions, writing the answer in its simplest form [e.g. $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$]
					6F5b	divide proper fractions by whole numbers [e.g. $\frac{1}{3} \div 2 = \frac{1}{6}$]
		4F6a recognise and write decimal equivalents to $\frac{1}{4}$, $\frac{3}{2}$, $\frac{1}{4}$	5F6a	read and write decimal numbers as fractions [e.g. $0.71 = \frac{71}{100}$]	6F6	associate a fraction with division to calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction [e.g. $\frac{3}{8}$]
		4F6b recognise and write decimal equivalents of any number of tenths or hundredths	5F6b	recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents		
		4F7 round decimals with one decimal place to the nearest whole number	5F7	round decimals with two decimal places to the nearest whole number and to one decimal place		
		4F8 compare numbers with the same number of decimal places up to two decimal places	5F8	read, write, order and compare numbers with up to three decimal places		

		Content dom	Content domain reference	
Strand	Year 3	Year 4	Year 5	Year 6
Fractions, decimals and percentages (continued)		find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths		identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places
				6F9b multiply one-digit numbers with up to twodecimal places by whole numbers
				6F9c use written division methods in cases where the answer has up to two-decimal places
	3F10 solve problems that involve 3F1–3F4	4F10a solve problems involving increasingly harder fractions to calculate quantities and fractions to divide quantities, including non-unit fractions where the answer is a whole number	5F10 solve problems involving numbers up to three decimal places	6F10 solve problems which require answers to be rounded to specified degrees of accuracy
		4F10b solve simple measure and money problems involving fractions and decimals to two decimal places		

				Content domain reference	in reference		
Strand		Year 3		Year 4	Year 5		Year 6
Ratio and proportion (continued)						6R4	solve problems involving unequal sharing and grouping using knowledge of fractions and multiples
Algebra						6A1	express missing number problems algebraically
						6A2	use simple formulae
						6A3	generate and describe linear number sequences
						6A4	find pairs of numbers that satisfy an equation with two unknowns
						6A5	enumerate possibilities of combinations of two variables
Measurement	3M1a	compare lengths (m/cm/mm)	4M1 c n	compare different measures, including money in pounds and pence			
	3M1b	compare mass (kg/g)					
	3M1c	compare volume/capacity (I/ml)					
	3M2a	measure lengths (m/cm/mm)	4M2 e n	estimate different measures, including money in pounds and pence			
	3M2b	measure mass (kg/g)					

Strand				Content domain reference	ain refe	rence	
		Year 3		Year 4		Year 5	Year 6
Measurement (continued)	3M2c	measure volume / capacity (I / ml)					
	M3	Key stage 1 content domain	i				
	3M4a	tell and write the time from an analogue clock; 12-hour clocks	4M4a	read, write and convert time between analogue and digital 12-hour clocks			
	3M4b	tell and write the time from an analogue clock; 24-hour clocks	4M4b	read, write and convert time between analogue and digital 24-hour clocks			
	3M4c	tell and write the time from an analogue clock, including using Roman numerals from I to XII	4M4c	solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days	5M4	solve problems involving converting between units of time	
	3M4d	estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock / a.m. / p.m., morning, afternoon, noon and midnight					
	3M4e	know the number of seconds in a minute and the number of days in each month, year and leap year					

-				Content domain reference	ain ref	erence		
Strand		Year 3		Year 4		Year 5		Year 6
Measurement (continued)	3M4f	compare durations of events, [e.g. to calculate the time taken by particular events or tasks]						
			4M5	convert between different units of measurement [e.g. kilometre to metre; hour to minute]	5M5	convert between different units of metric measure [e.g. kilometre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre]	6M5	use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation of up to three decimal places
					5M6	understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints	9W6	convert between miles and kilometres
	3M7	measure the perimeter of simple 2–D shapes	4M7a	measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres	5M7a	measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres	6M7a	recognise that shapes with the same areas can have different perimeters and vice versa

				Content domain reference	ain refe	rence		
Strand		Year 3		Year 4		Year 5		Year 6
Measurement (continued)	змэр	add and subtract lengths (m/cm/mm)			5M9b	use all four operations to solve problems involving measure [e.g. length] using decimal notation,		
	3M9c	add and subtract mass (kg/g)			5M9c	use all four operations to solve problems involving measure [e.g. mass] using decimal notation, including scaling		
	3M9d	add and subtract volume / capacity (l / ml)			5M9d	use all four operations to solve problems involving measure [e.g. volume] using decimal notation, including scaling		
Geometry –	G1 Wit	G1 Within key stage 1 content domain	nain					
shapes	3G2	identify horizontal, vertical lines and pairs of perpendicular and parallel lines	4G2a	compare and classify geometric shapes, including quadrilaterals and triangles based on their properties and sizes	5G2a	use the properties of rectangles to deduce related facts and find missing lengths and angles	6G2a	compare and classify geometric shapes based on their properties and sizes
			4G2b	identify lines of symmetry in 2–D shapes presented in different orientations	5G2b	distinguish between regular and irregular polygons based on reasoning about equal sides and angles	6G2b	describe simple 3–D shapes
			4G2c	complete a simple symmetric figure with respect to a specific line of symmetry				

				Content domain reference	ain refe	erence		
Strand		Year 3		Year 4		Year 5		Year 6
Geometry –	P1 Wi	P1 Within key stage 1 content domain	nain					ı
direction			4P2	describe movements between positions as translations of a given unit to the left / right and up / down	5P2	identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed	6P2	draw and translate simple shapes on the co-ordinate plane, and reflect them in the axes
			4P3a	describe positions on a 2–D grid as co-ordinates in the first quadrant			6P3	describe positions on the full co-ordinate grid (all four quadrants)
			4P3b	plot specified points and draw sides to complete a given polygon				
Statistics	351	interpret and present data using bar charts, pictograms and tables	451	interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs	551	complete, read and interpret information in tables, including timetables	651	interpret and construct pie charts and line graphs and use these to solve problems
	352	solve one-step and two- step questions [e.g. 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts, pictograms and tables	452	solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs	552	solve comparison, sum and difference problems using information presented in a line graph		
							683	calculate and interpret the mean as an average

4.3 Elements of the national curriculum that cannot be assessed fully

The table below identifies areas that are difficult to fully assess in a paper-based format. Some of the points below may be partially assessed.

Table 4: Elements of the curriculum that cannot be assessed fully

Content domain reference	Explanation
3C1, 5C1, 4C6, 5C5c, 5C6a, 6C6 and 6F11 – mental arithmetic skills	Mental mathematics skills cannot be directly assessed in a paper-based test since only the pupil's responses can be marked. For questions where only the answer is recorded, it is not possible to know the method that the pupil used or how quickly he or she completed the question.
	Pupils who are fluent with numbers will be able to use their mental arithmetic skills to find efficient strategies for completing calculations under test conditions. Therefore, good mental arithmetic skills will enable pupils to recall and apply number knowledge rapidly and accurately.
3G3b – make 3–D shapes using modelling materials	Requires practical equipment to assess validly.
5M8 – estimate capacity (e.g. using water)	Requires practical equipment to assess validly.

5. Cognitive domain

The cognitive domain seeks to make the thinking skills and intellectual processes required for the key stage 2 mathematics test explicit. Each question will be rated against the four strands of the cognitive domain listed in sections 5.1-5.4 below to provide an indication of the cognitive demand.

The cognitive domain will be used during test development to ensure comparability of demand as well as difficulty for tests in successive years. The national curriculum (2014) aims of solving mathematical problems, fluency and mathematical reasoning are reflected within the cognitive domain.

5.1 Depth of understanding

This strand is used to assess the demand associated with recalling facts and using procedures to solve problems.

Questions requiring less depth of understanding require simple procedural knowledge, such as the quick and accurate recall of mathematical facts or the application of a single procedure to solve a problem.

At intermediate levels of demand, a question may require the interpretation of a problem or application of facts and procedures. However, the component parts of these questions are simple and the links between the parts and processes are clear.

At a high level of demand, a greater depth of understanding is expected. Questions may require that facts and procedures will need to be used flexibly and creatively to find a solution to the problem.

Tabl	e 5:	Depth	of unc	lers	tandiı	ng
------	------	-------	--------	------	--------	----

Stupp d		Rating	g scale	
Strand	(low) 1	2	3	4 (high)
Depth of understanding	recall of facts or application of procedures	use facts and procedures to solve simple problems	use facts and procedures to solve more complex problems	understand and use facts and procedures creatively to solve complex or unfamiliar problems

5.2 Computational complexity

This strand is used to assess the computational demand of problems.

In questions with low complexity, there will be no numeric operation.

In questions with lower complexity, it is likely that a one-step process such as recalling a mathematical fact or the application of a simple procedure will be sufficient to solve the problem.

At an intermediate level of complexity, more than one numeric step or computation will be needed to solve the problem.

At a high level of complexity, questions will have multiple numeric steps or computations and the links between them within the problem will be complex.

Table 6: Computational complexity

Ctwo od		Rating	g scale	
Strand	(low) 1	2	3	4 (high)
Computational complexity	no numeric steps	one, or a small number of numeric steps	a larger number of numeric steps all steps are simple	a larger number of numeric steps, at least one of which is more complex

5.3 Spatial reasoning and data interpretation

This strand is used to assess the demand associated with the representation of geometrical problems involving 2-dimensional and 3-dimensional shapes and position and movement. This strand is also used to assess the demand associated with interpreting data presented in tables, pictograms, charts and graphs.

There is a low level of demand when all of the resources or information required to answer the question are presented within the problem (e.g. finding the perimeter of a shape by adding the length of the sides).

At intermediate levels of demand, spatial reasoning will be needed to manipulate the information presented in the question to solve the problem (e.g. reflect a polygon in a mirror line). Pupils may need to select the appropriate information in order to complete the problem (e.g. from a table, chart or graph).

At the highest level of demand there may be the need to use complex spatial reasoning to interpret, infer or generate new information from that given before the problem can be completed (such as identifying 3-dimensional characteristics from 2-dimensional representations or making inferences from the given information).

Table 7: Spatial reasoning and data interpretation

Ctuon d		Rating	g scale	
Strand	(low) 1	2	3	4 (high)
Spatial reasoning	no spatial reasoning required	manipulation of the geometric information is required	complex manipulation of the geometric information is required	interpret, infer or generate new geometric information
Data interpretation	no data interpretation required	select and retrieve information	select and interpret information	generate or infer new information from data

5.4 Response strategy

This strand describes the demand associated with constructing a response to a question.

At a low level of demand, the strategy for solving a problem is given as part of the presentation of the problem.

At a lower intermediate level of demand, the strategy for answering a problem is clear and following simple steps will lead to completion of the problem. Some reasoned construction may be associated with organising appropriate working.

At an upper intermediate level of demand there may be the need to construct a straightforward response. Some reasoned construction may be associated with organising more complex working.

At a high level of demand, the question will require that a strategy is developed and monitored to complete the task. The answer may need to be constructed, organised and reasoned.

Table 8: Response strategy

Stupp d		Rating	g scale	
Strand	(low) 1	2	3	4 (high)
Response strategy	select one or more responses or construct a simple response	construct a small set of responses	construct a straightforward explanation shows evidence of a method	construct a complex explanation

6. Test specification

This section provides details of each test component.

6.1 Summary

The test comprises two components, which will be presented to pupils as three separate papers.

Table 9: Format of the test

Component	Description	Number of papers	Number of marks	Timing of component
Paper 1: arithmetic	arithmetic assesses pupils confidence with the range of mathematical operations	1	40	30 minutes
Paper 2 and Paper 3: mathematical reasoning	mathematical fluency, solving mathematical problems and mathematical reasoning	2	70 overall 35 per paper	80 minutes 40 minutes per paper
	Total	3	110	110 minutes

6.2 Breadth and emphasis

The content and cognitive domains for the mathematics tests are specified in sections 4 and 5. The test will sample from the content domain in any given year. Although every element may not be included within each test, the full range of content detailed in this document will be assessed over time. Consolidation of the key stage 1 material is assumed within the key stage 2 programme of study and therefore material from key stage 1 may appear within the key stage 2 test. The questions in each test will be placed in an approximate order of difficulty.

The following sections show the proportion of marks attributed to each of the areas of the content and cognitive domains in a test.

6.2.1 Profile of content domain

Each of the nine strands listed in Table 10 will be tested on a yearly basis and these will be present in the tests in the ratios shown.

Table 10 shows the distribution of marks across the content domain.

Table 11 shows the distribution of marks across the components of the test and by national curriculum element.

Table 10: Profile of content domain

Content area Strand	Number of marks	Percentage of marks
Number, ratio and algebra	83–93	75–85%
Number, place value (N) Addition, subtraction, multiplication, division, calculations (C) Fractions, decimals and percentages (F) Ratio and proportion (R) Algebra (A)		
Measurement, geometry and statistics Measurement (M) Geometry – properties of shapes (G) Geometry – position and direction (P) Statistics (S)	17–27	15–25%

Table 11: Profile of marks by paper and national curriculum element

Paper	Number, ratio and algebra	Measurement, geometry and statistics	Total marks
Paper 1 (arithmetic)	40	0	40
Papers 2 and 3 (fluency, mathematical problem solving and mathematical reasoning)	22–26	9–13	70 (35 each paper)

6.2.2 Profile of cognitive domain

The cognitive domain is specified in section 5. Each test question will be rated in terms of demand against each of the four strands of the cognitive domain. The allocation of marks across each strand and demand rating is detailed in Table 12.

Table 12: Distribution of marks b	y cognitive domain strand
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Cognitive domain strand	(low) 1	2-3	4 (high)	Total marks
Depth of understanding	30–70	30–70	10–20	110
Computational complexity	0–30	60–100	10–20	110
Spatial reasoning and data interpretation	60–80	0–20	0–10	110
Response strategy	40–70	40–70	0–10	110

6.3 Format of questions and responses

6.3.1 Paper 1

Paper 1 (arithmetic) will comprise constructed response questions, presented as contextfree calculations. The majority of the arithmetic calculations will be worth one mark. However, two marks will be available for long multiplication and long division.

6.3.2 Papers 2 and 3

In Papers 2 and 3, mathematical problems are presented in a wide range of formats to ensure pupils can fully demonstrate mathematical fluency, mathematical problem solving and mathematical reasoning.

Papers 2 and 3 will include both selected response and constructed response questions.

Selected response questions, where pupils are required to select which option satisfies the constraint given in the question, will include question types such as:

- multiple choice, where pupils are required to select their response from the options given
- matching, where pupils are expected to indicate which options match correctly
- true / false or yes / no questions, where pupils are expected to choose one response for each statement or problem

Constructed response questions, where pupils are required to construct an answer rather than simply select one or more options, will include the following:

- constrained questions, where pupils are required to provide a single or best answer; these might involve giving the answer to a calculation, completing a chart or table, or drawing a shape; for questions worth more than one mark, partial credit will be available
- less constrained questions, where pupils are required to communicate their approach to evaluating a statement or problem

Questions in Papers 2 and 3 comprise both those presented in context and out of context. Up to 50 per cent of marks across these papers will be set in context.

6.4 Marking and mark schemes

The tests will be externally marked on screen by trained markers.

The mark schemes will give specific guidance for the marking of each question, together with general principles to ensure consistency of marking.

The mark schemes will provide the total number of marks available for each question and the criteria by which markers should award the marks to pupils' responses. Where multiple correct answers are possible, examples of different types of correct answers will be given in the mark schemes. Where applicable, additional guidance will indicate minimally acceptable responses and unacceptable responses. The mark schemes will provide a content domain reference, so it is possible to determine what is assessed in each question.

For all questions, the mark schemes will be developed during the test development process and will combine the expectations of experts with examples of pupils' responses obtained during trialling.

For multi-mark questions, where the correct answer has not been obtained, the mark scheme will indicate where marks are awarded either for using a formal method (Paper 1) or for correctly following a process or processes through the problem (Papers 2 and 3).

Partial marks will be awarded for correct working where the final answer is wrong but the pupil has used the formal method of working; where the grid method has been used for long multiplication or the 'chunking' method for long division, partial marks will not be awarded.

6.5 Reporting

The raw score on the test (the total marks achieved out of the 110 marks available) will be converted into a scaled score. Translating raw scores into scaled scores ensures performance can be reported on a consistent scale for all pupils. Scaled scores retain the same meaning from one year to the next. Therefore, a particular scaled score reflects the same standard of attainment in one year as in the previous year, having been adjusted for any differences in difficulty of the test.

Additionally, each pupil will receive an overall result indicating whether or not he or she has achieved the required standard on the test. A standard-setting exercise will be conducted on the first live test in 2016 in order to determine the scaled score needed for a pupil to be considered to have met the standard. This process will be facilitated by the performance descriptor in section 6.7 which defines the performance level required to meet the standard. In subsequent years, the standard will be maintained using appropriate statistical methods to translate raw scores on a new test into scaled scores with an additional judgemental exercise at the expected standard. The scaled score required to achieve the expected standard on the test will always remain the same.

6.6 Desired psychometric properties

While the focus of the outcome of the test will be whether a pupil has achieved the expected standard, the test must measure pupils' ability across the spectrum of attainment. As a result, the test must aim to minimise the standard error of measurement at every point on the reporting scale, particularly around the expected standard threshold.

The provision of a scaled score will aid in the interpretation of pupils' performance over time as the scaled score that represents the expected standard will be the same year-onyear. However, at the extremes of the scaled score distribution, as is standard practice, the scores will be truncated such that above and below a certain point, all pupils will be awarded the same scaled score in order to minimise the effect for pupils at the ends of the distribution, where the test is not measuring optimally.

6.7 Performance descriptor

This performance descriptor describes the typical characteristics of pupils whose performance in the key stage 2 tests is at the threshold of the expected standard. Pupils who achieve the expected standard in the tests have demonstrated sufficient knowledge to be well placed to succeed in the next phase of their education, having studied the full key stage 2 programme of study in mathematics. This performance descriptor will be used by a panel of teachers to set the standards on the new tests following their first administration in May 2016. It is not intended to be used to support teacher assessment since it reflects only the elements of the programme of study that can be assessed in a paper-based test (see the content domain in section 4).

6.7.1 Overview

Pupils working at the expected standard will be able to engage with all questions within the test. However, they will not always achieve full marks on each question, particularly if working at the threshold of the expected standard.

Questions will range from those requiring recall of facts or application of learned procedures to those requiring understanding of how to use facts and procedures creatively to decide how to solve complex and unfamiliar problems. There will be a variety of question formats including selected response, short answer and more complex calculations and explanations where the demonstration of an appropriate method may be rewarded.

Question difficulty will be affected by the strands of the cognitive domain such as computational complexity and spatial reasoning and data interpretation. This should be borne in mind when considering the remainder of this performance descriptor, since pupils working at the threshold of the expected standard may not give totally accurate or correct responses to questions. In cases where there are multiple interrelated computational steps and / or a need to infer new information or to visualise or represent an abstract problem, some pupils may find the question difficult to understand, especially in a test setting. This will be true even when the performance descriptor determines that a skill should be within the pupil's capacity if working at the expected standard.

The following sections describe the typical characteristics of pupils in Year 6 working at the threshold of the expected standard. It is recognised that different pupils will exhibit different strengths, so this is intended as a general guide rather than a prescriptive list. References in square brackets [] refer to aspects of the content domain as specified in section 4.

6.7.2 Number, ratio and algebra

Pupils working at the expected standard are able to:

- use place value in whole numbers up to 1 000 000 to compare and order numbers and are beginning to become confident with numbers up to 10 000 000 [N2, N3]
- round any whole number to the nearest power of ten [N4]
- use negative numbers in practical contexts such as temperature and calculate intervals across zero [N5]
- count forwards or backwards in steps of any whole number with one significant figure, e.g. 9, 20, 3000 [N1] to generate, describe and complete linear number sequences [A3]
- recognise and use multiples, factors, prime numbers less than 20 and square numbers up to 144 [C5]
- add and subtract whole numbers with up to two significant figures (e.g. 95 + 36, 5700 – 2900) [C1]
- add and subtract whole numbers with more than four digits, using formal written methods where appropriate [C2]
- use their understanding of place value to multiply and divide whole numbers and decimals with up to two decimal places by 10 or 100 (e.g. $1532 \div 100 = , \square \div 100 = 6.3$) [C6]
- multiply and divide whole numbers mentally drawing upon multiplication facts up to 12×12 and place value (e.g. 60×70) and begin to use these facts to work with larger numbers [C6]
- multiply numbers with up to two digits by a two digit number using the formal long multiplication method and becoming more confident with multiplication with larger numbers; multiply and divide numbers with up to four digits by a single digit number using the formal short division method and become more confident with division using larger numbers including the long division method. [C7]
- recognise and use equivalent fractions (e.g. $\frac{300}{900} = \frac{1}{3}$; $\frac{4}{5} = \frac{8}{10} = \frac{80}{100}$) [F2]
- recognise and use the equivalences between simple fractions, decimals and percentages (e.g. $0.3 = \frac{3}{10} = 30\%$) and becoming more confident with calculating other decimal fraction equivalents [F6, F11]
- find simple fractions and percentages of whole numbers and quantities (e.g. $\frac{2}{3}$ of 90; 20 × $\frac{1}{5}$; 30% of £60) [F1, F5, R2]
- add and subtract fractions with the same denominator, using mixed numbers where appropriate for the context (e.g. $1\frac{1}{5} \frac{2}{5} = \frac{6}{5} \frac{2}{5} = \frac{4}{5}$) [F2]

- add and subtract fractions with the same denominator and denominators that are multiples of the same number (e.g. $\frac{1}{4} + \frac{5}{8} = \frac{7}{8}$) and becoming more confident with more complex fraction calculations [F4]
- add and subtract decimal numbers that have the same number of decimal places (e.g. 157.31 – 29.16) [F10]
- multiply a one digit decimal number by a single digit number (e.g. 0.6×8) [F9]
- use simple ratio to compare quantities (e.g. Every pupil is given 3 pencils and a pen. 36 pencils were given out. How many pens were needed?) and estimate the distance from a map using a simple scale (e.g. where 1 cm represents 100 m) [R1, R3]
- use simple formulae expressed in words (e.g. time needed to cook a chicken: allow 20 minutes plus 40 minutes per kilogram) [A2]
- find possible values in missing number problems involving one or two unknowns (algebra) (e.g. Ben thinks of two numbers: the sum of the two numbers is 10: multiplied together they make 24: what are Ben's numbers? > (a + b=10, ab=24) [A1, A4]

6.7.3 Measurement

Pupils working at the expected standard are able to:

- read, write and convert time between analogue (including clock faces using Roman numerals) and digital 12 and 24– hour clocks, using a.m. and p.m. where necessary [M4]
- calculate the duration of an event using appropriate units of time (e.g. A film starts at 6:45p.m. and finishes at 8:05p.m. How long did it last?) [M4]
- convert between 'adjacent' metric units of measure for length, capacity and mass (e.g. 1.2 kg = 1200 g; how many 200 ml cups can be filled from a 2 litre bottle?; write 605 cm in metres) [M5]
- find the perimeter of compound shapes when all side lengths are known or can be easily determined (e.g. a simple shape made from two identical rectangles joined together to make an L-shape with given dimensions of the rectangle) [M7]
- calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm²) and square metres (m²) and estimate the area of irregular shapes by counting squares [M7]

6.7.4 Geometry

Pupils working at the expected standard are able to:

- compare and classify 3–D and 2–D shapes based on their properties (e.g. for 2–D shapes: parallel sides, length of sides, type and size of angles [G4], reflective symmetry [G2], regular / irregular polygons [G2]; for 3–D shapes: faces, vertices and edges) [G2]
- recognise and describe simple 3–D shapes, including using nets and other 2–D representations [G3]
- complete simple shapes using given lengths, such as 7.5cm, (accurate to ± -2 mm) and acute angles that are multiples of 5° (accurate to $\pm -2^{\circ}$) [G3]

- know and use the facts that angles at a point sum to 360°, angles at a point on a straight line sum to 180° and angles in a triangle sum to 180° (e.g. calculate the base angles of an isosceles triangle where the other angle is 110°) and identify other multiples of 90° [G4]
- identify, describe; and represent the position of a shape following a reflection or translation [P2]
- describe positions on a 2–D co-ordinate grid using axes with equal scales in the first quadrant (in the context of number or geometry) and use co-ordinates to complete a given rectangle; become more confident in plotting points in all four quadrants [P3]

6.7.5 Statistics

Pupils working at the expected standard are able to:

- complete, read and interpret information presented in tables and bar charts (e.g. find the difference between two bars showing temperatures, where one is 20°C and the other is 13°C, on a scale labelled in multiples of 5) [S1]
- interpret line graphs (e.g. begin to find the difference between two temperatures on a line graph, where one is 20°C and the other is 13°C, on a scale labelled in multiples of 5) and simple pie charts (e.g. a pie chart cut into eight pieces for favourite fruit using whole numbers for each section) [S1]
- calculate the mean as an average for simple sets of discrete data (e.g. find the mean mass of three parcels weighing 5 kg, 3 kg and 10 kg) [S3]

6.7.6 Solving problems and reason mathematically

Pupils working at the expected standard are able to:

- solve mathematical problems by applying their mathematics to a variety of routine and non-routine problems, in a range of contexts (including money and measures, geometry and statistics) using the content described above
- begin to reason mathematically making simple generalisations, using mathematical language
- use and interpret mathematical symbols and diagrams, and present information and results in a clear and organised way; for example:
 - solve mathematical problems with two or three computational steps using addition, subtraction, multiplication and division and a combination of these (e.g. extract and add prices from a table and calculate change, or solve problems such as 'Jason bought some bags of green apples (6 for 75p) and some bags of red apples (10 for 90p). He spent £4.20. How many bags of each type of apple did he buy?') [C4, C8]
 - solve mathematical problems involving numbers with up to two decimal places (e.g. find the two numbers which sum to 10 from this list: 0.01, 0.11, 1.01, 9.09, 9.9, 9.99) [F10, M9]
 - make simple connections between mathematical ideas
 - solve mathematical problems involving data [S2]

7. Diversity and inclusion

The Equality Act 2010 sets out the principles by which the national curriculum assessment and associated development activities are conducted. During the development of the tests, STA's test development division will make provision to overcome barriers to fair assessment for individuals and groups wherever possible.

National curriculum tests will also meet Ofqual's core regulatory criteria. One of the criteria refers to the need for assessment procedures to minimise bias: 'The assessment should minimise bias, differentiating only on the basis of each learner's ability to meet national curriculum requirements' (Regulatory framework for national assessment, published by Ofqual 2011).

The end of key stage 2 mathematics test should:

- use appropriate means to allow all pupils to demonstrate their mathematical fluency, solving problems and reasoning
- provide a suitable challenge for all pupils and give every pupil the opportunity to achieve as high a standard as possible
- provide opportunities for all pupils to achieve, irrespective of gender, disability or special educational need, social, linguistic or cultural backgrounds
- use materials that are familiar to pupils and for which they are adequately prepared
- not be detrimental to pupils' self-esteem or confidence
- be free from stereotyping and discrimination in any form

The test development process uses the principles of universal design, as described in the 'Guidance on the principles of language accessibility in national curriculum assessments' (New language accessibility guidance, published by Ofgual 2012).

In order to improve general accessibility for all pupils, where possible, questions will be placed in order of difficulty. As with all national curriculum tests, attempts have been made to make the question rubric as accessible as possible for all pupils, including those who experience reading and processing difficulties, and those for whom English is an additional language, while maintaining an appropriate level of demand to adequately assess the content. This includes applying the principles of plain English and universal design wherever possible, conducting interviews with pupils, and taking into account feedback from expert reviewers.

For each test in development, expert opinions on specific questions are gathered, for example, at inclusion panel meetings, which are attended by experts and practitioners from across the fields of disabilities and special educational needs. This provides an opportunity for some questions to be amended or removed in response to concerns raised.

Issues likely to be encountered by pupils with specific learning difficulties have been considered in detail. Where possible, features of questions that lead to construct irrelevant variance (for example, question formats and presentational features) have been considered and questions have been presented in line with best practice for dyslexia and other specific learning difficulties.

7.1 Access arrangements

The full range of access arrangements applicable to key stage 2 assessments as set out in the ARA will be available to eligible pupils as required.

Appendix: Glossary of terminology used in the test framework

cognitive domain	Cognitive processes refer to the thinking skills and intellectual processes that occur in response to a stimulus. The cognitive domain makes explicit the thinking skills associated with an assessment. The cognitive domain, as shown in this framework, also identifies other factors that may influence the difficulty of the questions.
component	A section of a test, presented to pupils as a test paper or test booklet. Some tests may have two or more components that each pupil needs to sit to complete the test. The key stage 2 mathematics test comprises two components.
construct irrelevant variance	Construct irrelevant variance is the variation in pupils' test scores that does not come from their knowledge of the content domain. It can result in pupils gaining fewer marks than their knowledge would suggest or lead to the award of more marks than their knowledge alone would deserve.
	The former can occur, for example, when questions in a mathematics test also unintentionally measure reading ability. The latter often occurs when unintended clues within questions allow pupils to answer correctly without having the required subject knowledge.
content domain	The body of subject knowledge to be assessed by the test.
distribution	The range of possible scaled scores.
domain	The codified definition of a body of skills and knowledge.
mark scheme	The document explaining the creditworthy responses or the criteria that must be applied to award the mark for a question in the test.
national curriculum programme of study	The statutory description of subject knowledge, skills and understanding for a given key stage. The key stage 1 and 2 programmes of study are published online at: https://www.gov.uk/government/publications/national-curriculum-in-england-primary-curriculum
performance descriptor	Description of the typical characteristics of pupils working at a particular standard. For these tests, the performance descriptor will characterise the minimum performance required to be working at the appropriate standard for the end of the key stage.

raw score	The unmodified score achieved on a test, following marking. In the case of these tests it is the total marks achieved.
	For example, if a pupil scores 27 out of 60 possible marks, the raw score is 27. Raw scores are often then converted to other measures such as percentile ranks, standardised scores or grades.
scaled score	A score which has been translated from a raw score into a score on a fixed, defined scale. This allows performance to be reported on a consistent scale for all pupils, which retains the same meaning from one year to the next. Therefore, a particular scaled score reflects the same level of attainment in one year as in the previous year, having been adjusted for any differences in difficulty of the specific tests.
standard	The required level of attainment in order to be classified into a particular performance category.
standard error of measurement	A reliability estimate that allows the user to determine a confidence interval around a test score. It is a measure of the distribution of scores that would be attained by a pupil had that pupil taken the test repeatedly under the same conditions.
standard setting	The process of applying the standard to a particular test to determine the score required for a pupil to be classified within a particular performance category.
test framework	A document that sets out the principles, rationale and key information about the test and contains a test specification.
test specification	A detailed description of what is to be included in a test in any single cycle of development.
truncate	To shorten by removing ends.

References

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About this publication

Who is it for?

This document is primarily aimed at those responsible for developing the key stage 2 national curriculum test in mathematics. It may also be of interest to schools with pupils in key stage 2 and other education professionals.

What does it cover?

Detailed information to ensure an appropriate test is developed, including the:

- content domain
- cognitive domain
- test specification
- test performance descriptors

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